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1. Two particles  $A$  and  $B$ , of mass 2 kg and 3 kg respectively, are moving towards each other in opposite directions along the same straight line on a smooth horizontal surface. The particles collide directly. Immediately before the collision the speed of  $A$  is  $5 \text{ m s}^{-1}$  and the speed of  $B$  is  $6 \text{ m s}^{-1}$ . The magnitude of the impulse exerted on  $B$  by  $A$  is  $14 \text{ N s}$ . Find

(a) the speed of  $A$  immediately after the collision, (3)

(b) the speed of  $B$  immediately after the collision. (3)



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2.

A diagram showing a triangle  $ABC$  with vertices  $A$  and  $B$  located on a horizontal line. Vertex  $C$  is positioned below the line. The angle at vertex  $A$  is labeled  $35^\circ$ , and the angle at vertex  $B$  is labeled  $25^\circ$ .

**Figure 1**

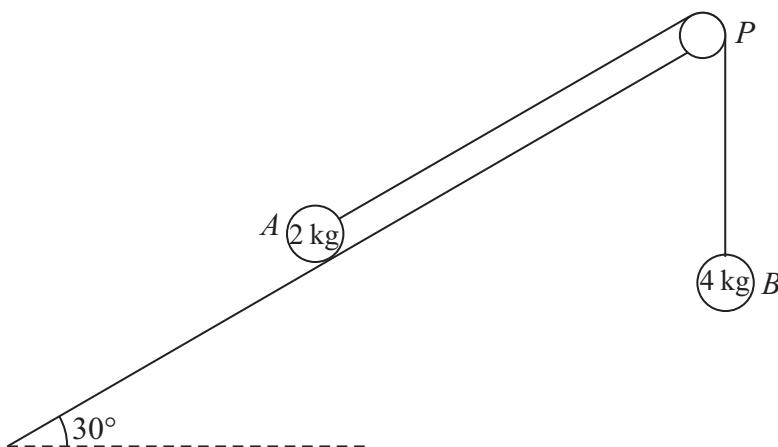
A particle of weight 8 N is attached at  $C$  to the ends of two light inextensible strings  $AC$  and  $BC$ . The other ends,  $A$  and  $B$ , are attached to a fixed horizontal ceiling. The particle hangs at rest in equilibrium, with the strings in a vertical plane. The string  $AC$  is inclined at  $35^\circ$  to the horizontal and the string  $BC$  is inclined at  $25^\circ$  to the horizontal, as shown in Figure 1. Find

- (i) the tension in the string  $AC$ ,
  - (ii) the tension in the string  $BC$ .

(8)



3.

**Figure 2**

A fixed rough plane is inclined at  $30^\circ$  to the horizontal. A small smooth pulley  $P$  is fixed at the top of the plane. Two particles  $A$  and  $B$ , of mass  $2\text{ kg}$  and  $4\text{ kg}$  respectively, are attached to the ends of a light inextensible string which passes over the pulley  $P$ . The part of the string from  $A$  to  $P$  is parallel to a line of greatest slope of the plane and  $B$  hangs freely below  $P$ , as shown in Figure 2. The coefficient of friction between  $A$  and the plane is  $\frac{1}{\sqrt{3}}$ . Initially  $A$  is held at rest on the plane. The particles are released from rest with the string taut and  $A$  moves up the plane.

Find the tension in the string immediately after the particles are released.

(9)

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### **Question 3 continued**

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4. At time  $t = 0$ , two balls  $A$  and  $B$  are projected vertically upwards. The ball  $A$  is projected vertically upwards with speed  $2 \text{ m s}^{-1}$  from a point  $50 \text{ m}$  above the horizontal ground. The ball  $B$  is projected vertically upwards from the ground with speed  $20 \text{ m s}^{-1}$ . At time  $t = T$  seconds, the two balls are at the same vertical height,  $h$  metres, above the ground. The balls are modelled as particles moving freely under gravity. Find

(a) the value of  $T$ ,

(5)

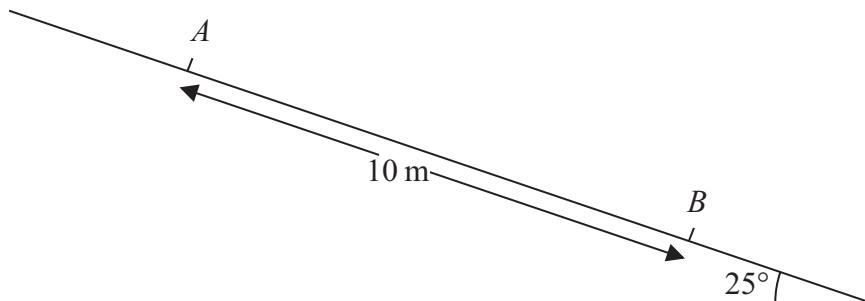
(b) the value of  $h$ .

(2)



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5.



**Figure 3**

A particle  $P$  of mass 0.6 kg slides with constant acceleration down a line of greatest slope of a rough plane, which is inclined at  $25^\circ$  to the horizontal. The particle passes through two points  $A$  and  $B$ , where  $AB = 10$  m, as shown in Figure 3. The speed of  $P$  at  $A$  is  $2 \text{ m s}^{-1}$ . The particle  $P$  takes 3.5 s to move from  $A$  to  $B$ . Find

- (a) the speed of  $P$  at  $B$ , (3)

(b) the acceleration of  $P$ , (2)

(c) the coefficient of friction between  $P$  and the plane. (5)



## **Question 5 continued**

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P 4 2 9 5 8 A 0 1 7 3 2

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6. [In this question **i** and **j** are horizontal unit vectors due east and due north respectively. Position vectors are given with respect to a fixed origin  $O$ .]

A ship  $S$  is moving with constant velocity  $(3\mathbf{i} + 3\mathbf{j})$  km h $^{-1}$ . At time  $t = 0$ , the position vector of  $S$  is  $(-4\mathbf{i} + 2\mathbf{j})$  km.

- (a) Find the position vector of  $S$  at time  $t$  hours.

(2)

A ship  $T$  is moving with constant velocity  $(-2\mathbf{i} + n\mathbf{j})$  km h $^{-1}$ . At time  $t = 0$ , the position vector of  $T$  is  $(6\mathbf{i} + \mathbf{j})$  km. The two ships meet at the point  $P$ .

- (b) Find the value of  $n$ .

(5)

- (c) Find the distance  $OP$ .

(4)



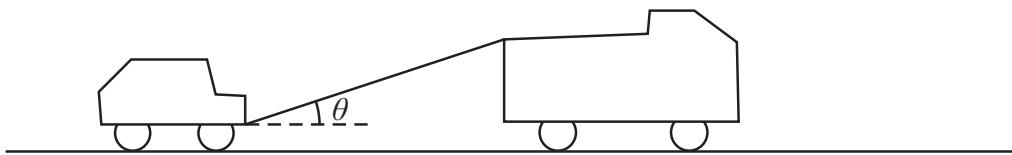
## **Question 6 continued**

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7.



**Figure 4**

A truck of mass 1750 kg is towing a car of mass 750 kg along a straight horizontal road. The two vehicles are joined by a light towbar which is inclined at an angle  $\theta$  to the road, as shown in Figure 4. The vehicles are travelling at  $20 \text{ m s}^{-1}$  as they enter a zone where the speed limit is  $14 \text{ m s}^{-1}$ . The truck's brakes are applied to give a constant braking force on the truck. The distance travelled between the instant when the brakes are applied and the instant when the speed of each vehicle is  $14 \text{ m s}^{-1}$  is 100 m.

- (a) Find the deceleration of the truck and the car.

(3)

The constant braking force on the truck has magnitude  $R$  newtons. The truck and the car also experience constant resistances to motion of 500 N and 300 N respectively. Given that  $\cos \theta = 0.9$ , find

- (b) the force in the towbar,

(4)

- (c) the value of  $R$ .

(4)



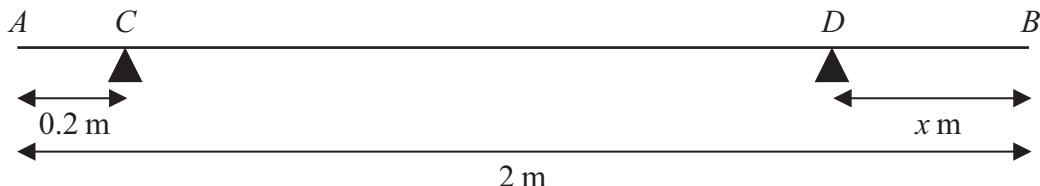
## **Question 7 continued**

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8.



**Figure 5**

A uniform rod  $AB$  has length 2 m and mass 50 kg. The rod is in equilibrium in a horizontal position, resting on two smooth supports at  $C$  and  $D$ , where  $AC = 0.2$  metres and  $DB = x$  metres, as shown in Figure 5. Given that the magnitude of the reaction on the rod at  $D$  is twice the magnitude of the reaction on the rod at  $C$ ,

- (a) find the value of  $x$ .

(6)

The support at  $D$  is now moved to the point  $E$  on the rod, where  $EB = 0.4$  metres. A particle of mass  $m$  kg is placed on the rod at  $B$ , and the rod remains in equilibrium in a horizontal position. Given that the magnitude of the reaction on the rod at  $E$  is four times the magnitude of the reaction on the rod at  $C$ ,

- (b) find the value of  $m$ .

(7)



**Question 8 continued**Leave  
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